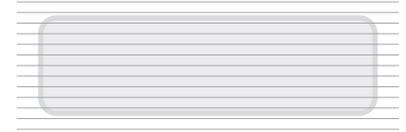




Test 42

Name \_\_\_\_\_ Uni \_\_\_\_\_



[1] Find the general solution to the following system of equations.

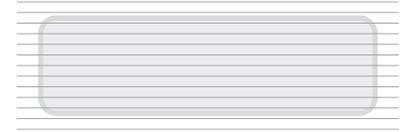
$$\begin{bmatrix} 1 & 1 & 1 & 2 & 1 \\ 1 & 1 & 2 & 1 & 1 \\ 1 & 2 & 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} v \\ w \\ x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 1 \\ -1 \\ 0 \end{bmatrix}$$

$$\begin{bmatrix} v \\ w \\ x \\ y \\ z \end{bmatrix} =$$



Test 91

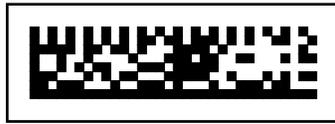
Name \_\_\_\_\_ Uni \_\_\_\_\_



[1] Find the general solution to the following system of equations.

$$\begin{bmatrix} 5 & 7 & 1 & 2 \\ 3 & 4 & 1 & 1 \\ 2 & 3 & 0 & 1 \end{bmatrix} \begin{bmatrix} w \\ x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 3 \\ 2 \\ 1 \end{bmatrix}$$

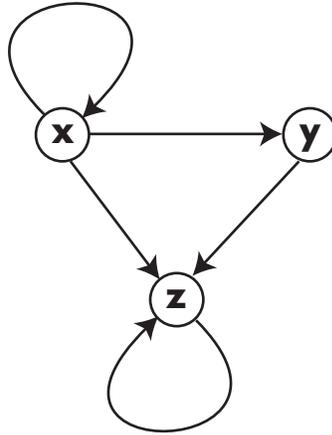
$$\begin{bmatrix} w \\ x \\ y \\ z \end{bmatrix} =$$



Exam 08

exam08b1p2

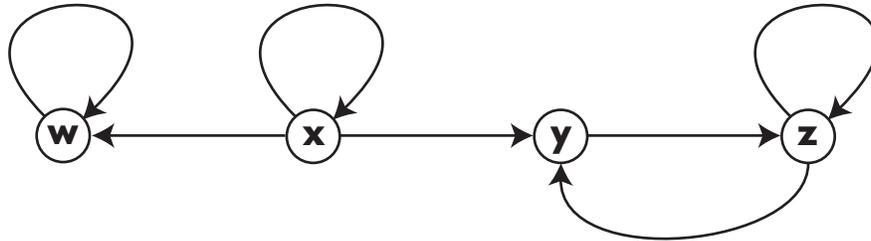
[2] Using matrix multiplication, count the number of paths of length eight from  $x$  to  $z$ .





Test 30

[2] Using matrix multiplication, count the number of paths of length ten from  $x$  to  $z$ .



number of paths =



Test 36

[4] Find the  $2 \times 2$  matrix  $A$  that reflects across the line  $2y = 3x$ .

$$A = \frac{1}{\square} \begin{bmatrix} \square & \square \\ \square & \square \end{bmatrix}$$



Test 42

[4] Find the  $2 \times 2$  matrix  $A$  that reflects across the line  $4y = x$ .

$$A = \frac{1}{\square} \begin{bmatrix} \square & \square \\ \square & \square \end{bmatrix}$$



Test 30

[3] Express  $A$  as a product of four elementary matrices, where

$$A = \begin{bmatrix} 2 & 1 \\ 5 & 3 \end{bmatrix}$$

$$A = \begin{bmatrix} \square & \square \\ \square & \square \end{bmatrix} \begin{bmatrix} \square & \square \\ \square & \square \end{bmatrix} \begin{bmatrix} \square & \square \\ \square & \square \end{bmatrix} \begin{bmatrix} \square & \square \\ \square & \square \end{bmatrix}$$



exam03a1p4

**Exam 03**

[4] Find the matrix  $A$  such that

$$A \begin{bmatrix} 1 & 1 & 0 \\ 0 & 1 & 1 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 2 & 1 \\ 1 & 1 & 1 \\ 1 & 2 & 2 \end{bmatrix}$$

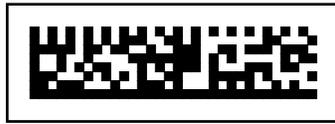


Test 42

[3] Find the intersection of the following two affine subspaces of  $\mathbb{R}^3$ .

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 1 \\ 0 \\ 1 \end{bmatrix} + \begin{bmatrix} 1 & 0 \\ 1 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} q \\ r \end{bmatrix}, \quad \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix} + \begin{bmatrix} 0 & 1 \\ 1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} s \\ t \end{bmatrix}$$

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} =$$



exam08b1p5

Exam 08

[5] Find the intersection of the following two affine subspaces of  $\mathbb{R}^4$ .

$$\begin{bmatrix} 1 & 1 & 1 & -2 \\ 1 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} w \\ x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 0 \\ 4 \end{bmatrix}$$

$$\begin{bmatrix} w \\ x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \end{bmatrix} + \begin{bmatrix} 1 & 1 \\ -1 & 1 \\ 1 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} r \\ s \end{bmatrix}$$