



Test 1

Name \_\_\_\_\_ Uni \_\_\_\_\_

[1] Find the intersection of the following two affine subspaces of  $\mathbb{R}^3$ .

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \\ -1 \end{bmatrix} t$$

$$x + z = 3$$

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} =$$



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[2] Find the inverse to the matrix

$$A = \begin{bmatrix} 1 & 3 & 4 \\ 2 & 2 & 3 \\ 0 & 1 & 2 \end{bmatrix}$$

$$A^{-1} = \frac{1}{+ \boxed{\phantom{00}}} \begin{bmatrix} \boxed{\phantom{00}} & \boxed{\phantom{00}} & \boxed{\phantom{00}} \\ \boxed{\phantom{00}} & \boxed{\phantom{00}} & \boxed{\phantom{00}} \\ \boxed{\phantom{00}} & \boxed{\phantom{00}} & \boxed{\phantom{00}} \end{bmatrix}$$



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[3] Find  $A^n$  where  $A$  is the matrix

$$A = \begin{bmatrix} 0 & 2 \\ 3 & -1 \end{bmatrix}$$

$$A^n = \frac{\begin{array}{|c|} \hline \square \\ \hline \square \end{array}}{\begin{array}{|c|} \hline \square \\ \hline \square \end{array}} \begin{bmatrix} \square & \square \\ \square & \square \end{bmatrix} + \frac{\begin{array}{|c|} \hline \square \\ \hline \square \end{array}}{\begin{array}{|c|} \hline \square \\ \hline \square \end{array}} \begin{bmatrix} \square & \square \\ \square & \square \end{bmatrix}$$



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[4] Find  $A^n$  where  $A$  is the matrix

$$A = \begin{bmatrix} -3 & 2 \\ -2 & 1 \end{bmatrix}$$

$$A^n = \frac{\begin{array}{|c|} \hline \square \\ \hline \end{array}}{\begin{array}{|c|} \hline \square \\ \hline \end{array}} \begin{bmatrix} \square & \square \\ \square & \square \end{bmatrix} + \frac{\begin{array}{|c|} \hline \square \\ \hline \end{array}}{\begin{array}{|c|} \hline \square \\ \hline \end{array}} \begin{bmatrix} \square & \square \\ \square & \square \end{bmatrix}$$



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[5] Find  $A^n$  where  $A$  is the matrix

$$A = \begin{bmatrix} 1 & 1 & 0 \\ 1 & 1 & 0 \\ 2 & 1 & 1 \end{bmatrix}$$

$$A^n = \frac{\begin{bmatrix} \square & \square & \square \\ \square & \square & \square \end{bmatrix}}{\begin{bmatrix} \square & \square & \square \\ \square & \square & \square \end{bmatrix}} + \frac{\begin{bmatrix} \square & \square & \square \\ \square & \square & \square \end{bmatrix}}{\begin{bmatrix} \square & \square & \square \\ \square & \square & \square \end{bmatrix}} + \frac{\begin{bmatrix} \square & \square & \square \\ \square & \square & \square \end{bmatrix}}{\begin{bmatrix} \square & \square & \square \\ \square & \square & \square \end{bmatrix}}$$



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[6] Find  $e^{At}$  where  $A$  is the matrix

$$A = \begin{bmatrix} 2 & 2 & 1 \\ -1 & -2 & -2 \\ 1 & 3 & 3 \end{bmatrix}$$

$$e^{At} = \frac{\begin{bmatrix} \square & \square \\ \square & \square \end{bmatrix}}{\begin{bmatrix} \square & \square \\ \square & \square \end{bmatrix}} \begin{bmatrix} \square & \square & \square \\ \square & \square & \square \\ \square & \square & \square \end{bmatrix} + \frac{\begin{bmatrix} \square & \square \\ \square & \square \end{bmatrix}}{\begin{bmatrix} \square & \square \\ \square & \square \end{bmatrix}} \begin{bmatrix} \square & \square & \square \\ \square & \square & \square \\ \square & \square & \square \end{bmatrix} + \frac{\begin{bmatrix} \square & \square \\ \square & \square \end{bmatrix}}{\begin{bmatrix} \square & \square \\ \square & \square \end{bmatrix}} \begin{bmatrix} \square & \square & \square \\ \square & \square & \square \\ \square & \square & \square \end{bmatrix}$$



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[7] Solve the differential equation  $y' = Ay$  where

$$A = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 2 & 0 \\ 0 & 1 & 2 \end{bmatrix}, \quad y(0) = \begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix}$$

$$y = \frac{\begin{bmatrix} \phantom{0} \\ \phantom{0} \end{bmatrix}}{\begin{bmatrix} \phantom{0} \end{bmatrix}} \begin{bmatrix} \phantom{0} \\ \phantom{0} \\ \phantom{0} \end{bmatrix} + \frac{\begin{bmatrix} \phantom{0} \\ \phantom{0} \end{bmatrix}}{\begin{bmatrix} \phantom{0} \end{bmatrix}} \begin{bmatrix} \phantom{0} \\ \phantom{0} \\ \phantom{0} \end{bmatrix} + \frac{\begin{bmatrix} \phantom{0} \\ \phantom{0} \end{bmatrix}}{\begin{bmatrix} \phantom{0} \end{bmatrix}} \begin{bmatrix} \phantom{0} \\ \phantom{0} \\ \phantom{0} \end{bmatrix}$$



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[8] Express the quadratic form

$$2x^2 - 2xy + 3y^2 + 2yz + 2z^2$$

as a sum of squares of orthogonal linear forms.

$\boxed{\phantom{000}} \left( \boxed{\phantom{000000}} \right)^2 + \boxed{\phantom{000}} \left( \boxed{\phantom{000000}} \right)^2 + \boxed{\phantom{000}} \left( \boxed{\phantom{000000}} \right)^2$
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