[1] Find the 2 × 2 matrix which reflects across the line 3x - y = 0.

[2] Find the 3 × 3 matrix which vanishes on the plane 4x + 2y + z = 0, and maps the vector (1, 1, 1) to itself.

[3] Find the 3×3 matrix which vanishes on the vector (1, 1, 0), and maps each point on the plane x + 2y + 2z = 0 to itself.

[4] Find the 3 \times 3 matrix that projects orthogonally onto the line

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 1 \\ -2 \\ 3 \end{bmatrix} t$$

[5] Find the 3 \times 3 matrix that projects orthogonally onto the plane

$$x + 2y + 3z = 0$$

[6] Find the row space and the column space of the matrix

$$\begin{bmatrix} 0 & 0 & 1 & 1 & 1 & 1 \\ 0 & 0 & 1 & 2 & 3 & 4 \\ 0 & 0 & 1 & 3 & 6 & 10 \end{bmatrix}$$

[7] By least squares, find the equation of the form y = ax + b that best fits the data

$\int x_1$	y1 _		0	1	
χ_2	y_2	=	1	0	
x_3	y ₃ _		2	3_	

[8] Find an orthogonal basis for the subspace V of \mathbb{R}^4 spanned by the vectors

(1, 2, 0, 0) (0, 1, 2, 0) (1, 3, 3, 2) (0, 0, 1, 2) (1, 3, 3, 2)

Extend this basis to an orthogonal basis for \mathbb{R}^4 .

[9] Let V be the vector space of all polynomials of degree ≤ 2 in the variable x with coefficients in \mathbb{R} . Let W be the subspace consisting of those polynomials f(x) such that f(-1) = 0. Find the orthogonal projection of the polynomial x + 1 onto the subspace W, with respect to the inner product

$$\langle f,g\rangle = \int_0^1 f(x)g(x) dx$$