## Math 222 in class problems Week: March 1, 2021

1. Evaluate

$$
\int_{-2}^{2} \int_{-\sqrt{4-x^{2}}}^{\sqrt{4-x^{2}}} \int_{\sqrt{x^{2}+y^{2}}}^{2} x^{2}+y^{2} d z d y d x
$$

2. Find the volume of the region lying between the planes $z=0$ and $z=4-x$, outside the cylinder with base $r=2 \cos \theta$, and inside the cylinder with base $(x-2)^{2}+y^{2}=4$.
3. Set up the integral representing the volume of the solid region bounded between $z=4$, $z=1-x^{2}-y^{2}$, which is inside $x^{2}+y^{2}=1$.
4. HW \#5 4b)

Sketch the solid whose volume is given by the integral and evaluate the integral

$$
\int_{0}^{\pi / 4} \int_{0}^{2 \pi} \int_{0}^{\sec \varphi} \rho^{2} \sin \varphi d \rho d \theta d \varphi
$$

5. Graph the region of integration and convert to spherical coordinates in order to evaluate (but do not do so):

$$
\int_{0}^{3} \int_{0}^{\sqrt{9-y^{2}}} \int_{\sqrt{x^{2}+y^{2}}}^{\sqrt{18-x^{2}-y^{2}}} x^{2}+y^{2}+z^{2} d z d x d y
$$

