Math 222 in class problems Week: February 22, 2021

1. Stewart

Evaluate

$$
\int_{0}^{2} \int_{-\sqrt{4-x^{2}}}^{0} \frac{2}{1+x^{2}+y^{2}} d y d x
$$

2. Folland

Find the area of the region inside the cardiod $r=1+\cos \theta$
3. University of Wisconsin - Madison Midterm

Use a triple integral to find the volume of the tetrahedron in the first octant $(x \geq 0, y \geq$ $0, z \geq 0)$ bounded by the coordinate planes passing through the points $(1,0,0),(0,2,0)$, $(0,0,3)$.
4. Folland

Let $S \subset \mathbb{R}^{3}$ be the region between the paraboloid $z=x^{2}+y^{2}$ and the plane $z=1$. Express the triple integral $\iiint_{S} f d V$ as an iterated integral with the order of integration:
(a) $d V=d z d y d x$
(b) $d V=d y d z d x$
(c) $d V=d x d y d z$

