Math 222 in class problems

1. Stewart Evaluate

$$\int_0^2 \int_{-\sqrt{4-x^2}}^0 \frac{2}{1+x^2+y^2} \, dy dx$$

2. Folland

Find the area of the region inside the cardiod $r = 1 + \cos \theta$

3. University of Wisconsin - Madison Midterm

Use a triple integral to find the volume of the tetrahedron in the first octant $(x \ge 0, y \ge 0, z \ge 0)$ bounded by the coordinate planes passing through the points (1,0,0), (0,2,0), (0,0,3).

4. Folland

Let $S \subset \mathbb{R}^3$ be the region between the paraboloid $z = x^2 + y^2$ and the plane z = 1. Express the triple integral $\iiint_S f \, dV$ as an iterated integral with the order of integration:

- (a) $dV = dz \, dy \, dx$
- (b) dV = dy dz dx
- (c) dV = dx dy dz