

Algebraic topology

Homework 9. Due Monday, December 4.

Exercise 41 at the end of section 2.2.

Exercises 1, 2, 5, 6, 10 for section 3.1.

1. Compute homology groups (with coefficients in \mathbb{Z} and \mathbb{Z}_p for all primes p) of $\mathbb{C}\mathbb{P}^n \times \mathbb{C}\mathbb{P}^m$, $\mathbb{C}\mathbb{P}^n \times \mathbb{R}\mathbb{P}^m$, and $\mathbb{R}\mathbb{P}^n \times \mathbb{R}\mathbb{P}^m$. What are Euler characteristics of these spaces?

2. Check that any two free resolutions $0 \rightarrow F_1 \rightarrow F_0 \rightarrow 0$ of an abelian group G are chain homotopy equivalent.