For a given sharp functional or geometric inequality, the question of stability asks the following: if a set or function almost attains equality in the inequality, then is it close, in a suitable sense, to one of the equality cases? We discuss stability results for the Sobolev inequality on  $\mathbb{R}^n$  for  $p \ge 2$ , based on joint work with A. Figalli, and for the anisotropic isoperimetric inequality.