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\[ C \quad D \quad E \quad F \quad G \quad H \quad I \quad J \quad K \quad L \quad M \quad N \quad P \quad Q \quad R \quad S \]
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\[ E \ F \ G \ H \ I \ J \ K \ L \ M \ N \ P \ Q \ R \ S \ T \ U \]
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\[
\begin{array}{cccc}
D & E & F & G \\
H & I & J & K \\
L & M & N & P \\
Q & R & S & T \\
\end{array}
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\[
G \quad H \quad I \quad J \quad K \quad L \quad M \quad N \quad P \quad Q \quad R \quad S \quad T \quad U \quad V \quad W
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\[
H \ I \ J \ K \ L \ M \ N \ P \ Q \ R \ S \ T \ U \ V \ W \ X
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\[
\begin{array}{cccc}
\hspace{1cm} & \hspace{1cm} & \hspace{1cm} & \hspace{1cm} \\
\hspace{1cm} & \hspace{1cm} & \hspace{1cm} & \hspace{1cm} \\
\hspace{1cm} & \hspace{1cm} & \hspace{1cm} & \hspace{1cm} \\
\hspace{1cm} & \hspace{1cm} & \hspace{1cm} & \hspace{1cm} \\
\end{array}
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A B C D E F G H I J K L M N P Q
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\[
\begin{array}{|c|c|c|c|}
\hline
\text{Action 1} & \text{Action 2} & \text{Action 3} & \text{Action 4} \\
\hline
\text{Pattern 1} & \text{Pattern 2} & \text{Pattern 3} & \text{Pattern 4} \\
\hline
\end{array}
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Practice First Exam AK
MATH V1010: Groups and Symmetry, September 25, 2003

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Diagram:

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\[
\begin{align*}
\text{F} & \quad \text{G} & \quad \text{H} & \quad \text{I} & \quad \text{J} & \quad \text{K} & \quad \text{L} & \quad \text{M} & \quad \text{N} & \quad \text{P} & \quad \text{Q} & \quad \text{R} & \quad \text{S} & \quad \text{T} & \quad \text{U} & \quad \text{V}
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Practice First Exam BA
MATH V1010: Groups and Symmetry, September 25, 2003

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