

MATH W4051 PROBLEM SET 9
DUE NOVEMBER 24, 2009.

INSTRUCTOR: ROBERT LIPSHITZ

- (1) Munkres 74.1
- (2) Munkres 74.6
- (3) Munkres 75.3
- (4) Munkres 53.4
- (5) Munkres 53.5
- (6) Munkres 54.1
- (7) Munkres 54.5
- (8) A group G is *finitely presented* if $G \cong \langle a_1, \dots, a_n \mid r_1, \dots, r_m \rangle$ for some n and words r_1, \dots, r_m in a_1, \dots, a_n . Prove that for any finitely presented group G there is a path-connected space X so that $\pi_1(X) \cong G$.

(Hint: take a bouquet of circles $\bigvee_{i=1}^n S^1$, one for each generator, and then glue on disks according to the relations. You might find it easier to glue on the disks one at a time, and use induction.)

E-mail address: r12327@columbia.edu