## Lie Groups and Representations, Fall 2013 Problem Set 4

## Due Monday, November 11

**Problem 1:** Kirillov Problem 4.2

**Problem 2:** Kirillov Problem 4.3

**Problem 3:** Kirillov Problem 4.9

**Problem 4:** Kirillov Problem 4.13

**Problem 5:** Prove the Frobenius reciprocity relation for induced representations (just do for finite groups): when H is a subgroup of G,  $(\rho, W)$  a representation of H, one has an induced representation

$$Ind_H^G(W)$$

and

$$Hom_G(V, Ind_H^G(W)) = Hom_H(V, W)$$

where V is an arbitrary representation of G, and on the right-hand side V refers to its restriction as a representation of H