

Speaker: A. Raghuram

Title: Special values of automorphic L-functions and congruences

Abstract: Hida proved in 1981 that if a prime p divides the algebraic part of the value at $s = 1$ of the adjoint L-function of a holomorphic cusp form f , then there is another cusp form g such that f is congruent to g modulo the prime p . This result was generalized to Hilbert modular forms by Eknath Ghate and Mladen Dimitrov, and to certain cusp forms on $GL(2)$ over an imaginary quadratic field by Eric Urban, and recently to cusp forms on $GL(2)$ over any number field by Namikawa. In this talk, I will discuss further generalizations of this phenomenon to the context adjoint L-values for cohomological cuspidal automorphic representations of $GL(n)$ over any number field. This is a report of joint work with Baskar Balasubramanyam. In Part 1, I will introduce the students/postdocs to the general topic of special values of L-functions and show, with some $GL(2)$ examples, how one tries to study the arithmetic of L-functions. In the colloquium style research talk I will give an overview of my project as above but without any proofs, and in the concluding part I hope to sketch some proofs.